



# Geodesy Primer: Datums & Projections

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# Training Agenda

- 9:00 to 11:00 (Break @ 10:00):
- 2:00 to 4:00 (Break @ 3:00):
- Introductions
- Geodesy
  - Coordinate Systems
  - Datum Transformations
  - Map Projections



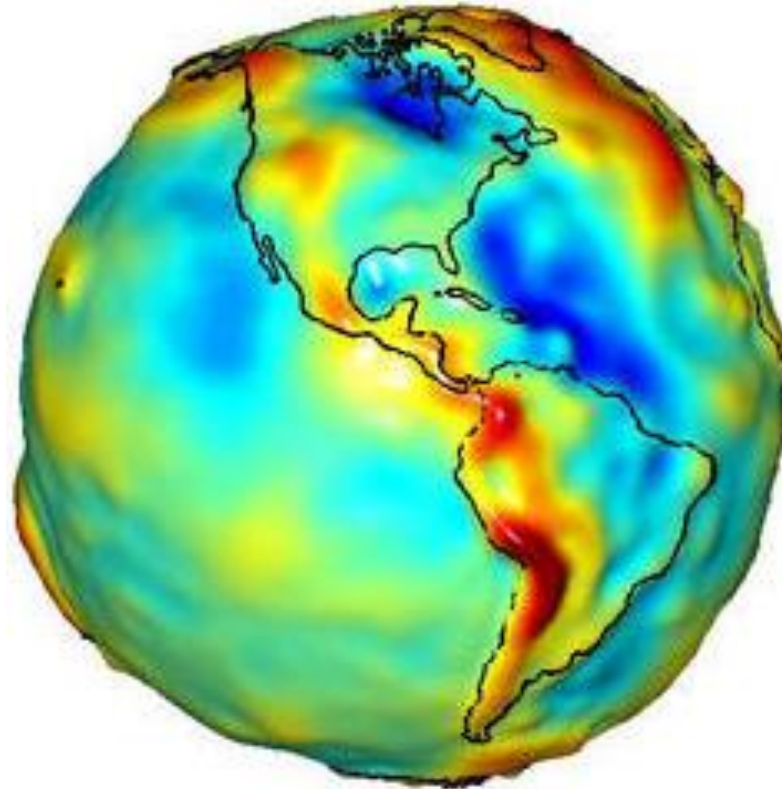
## What is Geodesy?

- The science of measuring the size and shape of the Earth
- Determination of the exact position of points on its surface
- *How that changes over time*



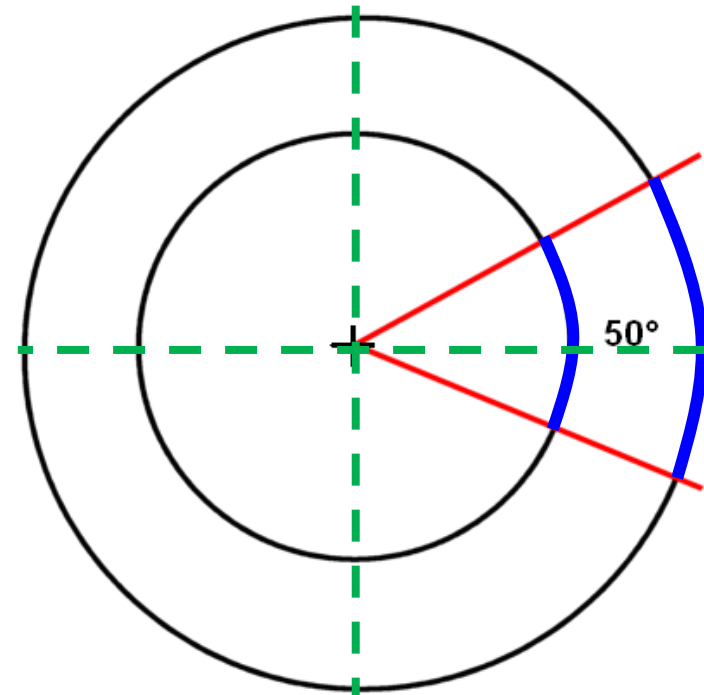
# Size & Shape

- Earth is a *Pseudo-spheroid* roughly 6,357km in radius
  - It's wider at the Equator than the poles
  - The surface undulates



# Coordinates

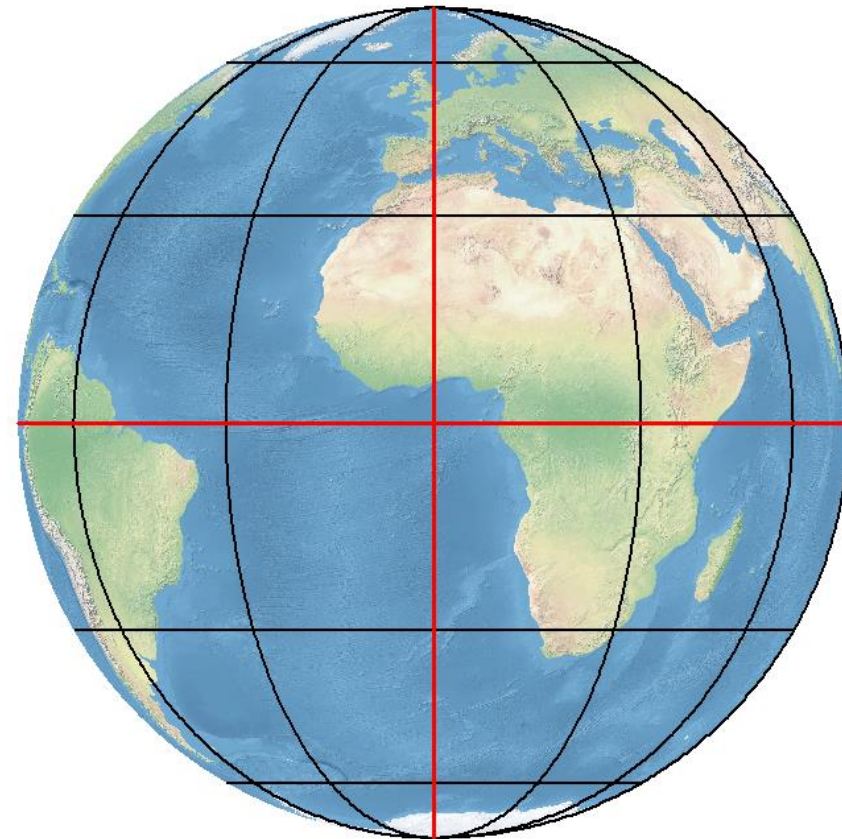
- What are Coordinates?
  - A set of numbers used to represent points in space
  - Measures relative to an **Origin** and Axes
  - Depending on the coordinate system, coordinates can be displayed in various formats of various units.
- Units
  - Angular
    - In Geodetic Coordinate Systems, coordinates are given in angular units, the most common being Degrees.
    - Angular units can be displayed in a number of formats
  - Linear
    - Cartesian and Projected coordinate systems use linear measures
    - Unit format is mostly limited to decimal precision.



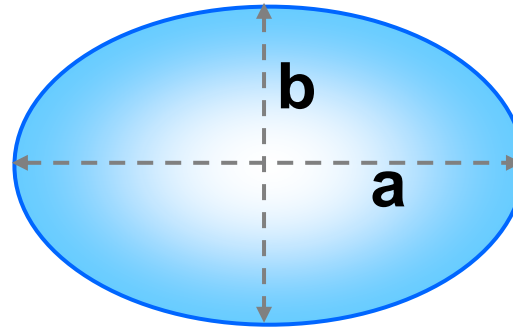


# Geodetic Coordinate Systems

- Globes are the most accurate maps we have
- All geodetic systems use Latitude and Longitude to define the positions on the Earth. These are angular measurements, not linear
- The two main reference lines from which all distances and locations are calculated are the **Equator** and the **Prime Meridian**

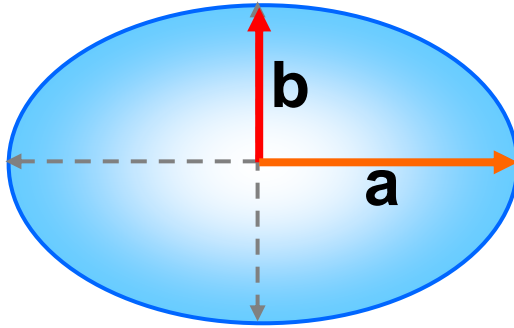


# Ellipsoid



- Sir Isaac Newton popularised the non-spherical shape of the Earth into public awareness. He concluded that the Earth was an “oblate ellipsoid of revolution” – an ellipse wider at the equator than at the poles.
- At the equator, the diameter of the Earth is ~7927 miles (~12,756km). At the poles, the diameter is almost 7900 miles (12,713km). 27 miles, a difference of 0.34% is just enough to give map makers a headache.
- If it weren't for Flattening, mapping would be as easy as **Pi**.

# Flattening



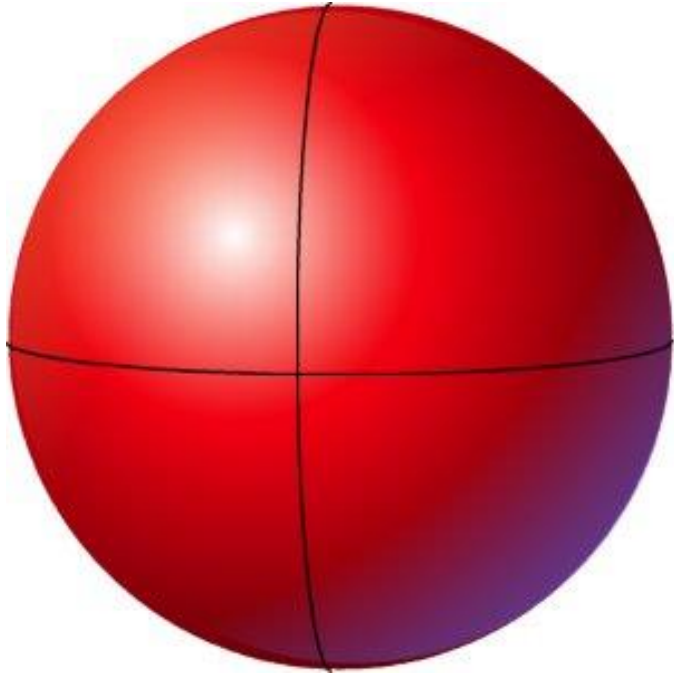
Flattening is the ratio of the difference between the Semi-Major Axis, and the Semi-Minor Axis.

$$f = (a - b) / a$$
$$1/f = a / (a - b)$$

Ellipsoid	Radius to Equator	1/f	Region
Plessis 1817	6,376,523 meters	308.64	France
Bessel 1841	6,377,397 meters	299.15	Japan
Airy 1830	6,377,563 meters	299.32	UK
GRS80/WGS84	6,378,137 meters	298.26	World
Clarke 1866	6,378,206 meters	294.98	North America
Clarke 1880	6,378,206 meters	293.46	France, Africa
SLC95	6,378,523 meters	298.28	St Louis County, MN



# Horizontal Datums

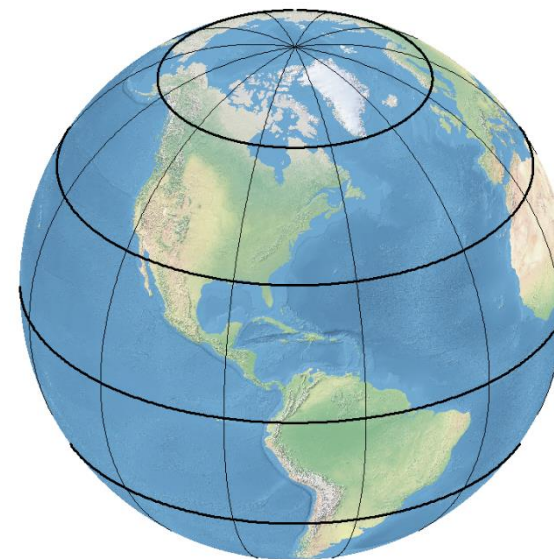
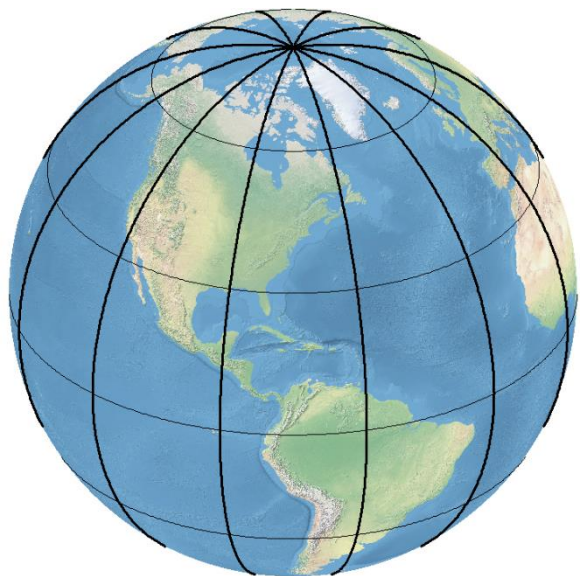


- A datum is a “mappable surface” defined by an ellipsoid with a base-point and a reference meridian.
  - A datum takes your ellipsoid and gives it an origin, tying it to the earth at one spot.
  - One point on the Earth can have many different coordinates, depending on the datum being used.
- 
- You can have an ellipsoid without it being a datum.
  - You **CAN NOT** have a datum without an ellipsoid!

# The Equator & Prime Meridian

## The Equator

- The Equator divides the Earth in half with an imaginary line that runs East/West around the middle of the globe.
- All similar lines running parallel to the equator at constant increments are called lines of **Latitude**.
- Also referred to as parallels, they run 90 degrees north and 90 degrees south of the equator and they never intersect with each other.



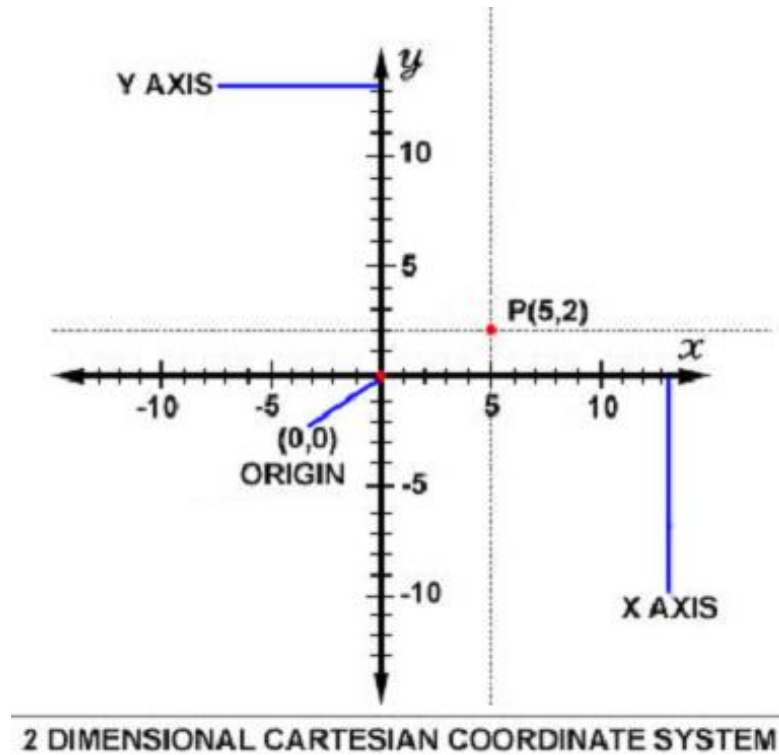
## The Prime Meridian

- The Prime Meridian is a mostly imaginary (and arbitrary) line that runs North/South, dividing the Earth in half from pole to pole. (Est. 1851 by Sir George Airy; standardized in 1884.)
- It runs through the Royal Observatory of Greenwich, England and is also known as the *Greenwich Meridian*.
- All similar lines running North/South through the poles are called lines of **Longitude**.
- They are farthest apart at the equator and converge at the poles.

# Degrees

- How “Big” is a Degree?
  - One degree of **longitude** on the surface of Earth at the equator is approximately 69.17mi (111.32km)
  - At the North/South Pole, it is 0 miles
  - Degrees are not constant distances on the surface like linear measurements
- Different Formats
  - Degrees Minutes Seconds, Decimal Minutes, Decimal Degrees are some of the more common degree formats
  - **44° 13' 36.96" N, 69° 46' 29.11" W**      Degrees Minutes Seconds
  - **44° 13.616', -69° 46.485'**      Decimal Minutes
  - **44.226933, -69.774753**      Decimal Degrees
  - **44.133696, -69.462911**      DMS
  - **44.136160, -69.464851**      DM
  - **44133696, -069462911**      Packed DMS
  - **44136160, -069464851**      Packed DM

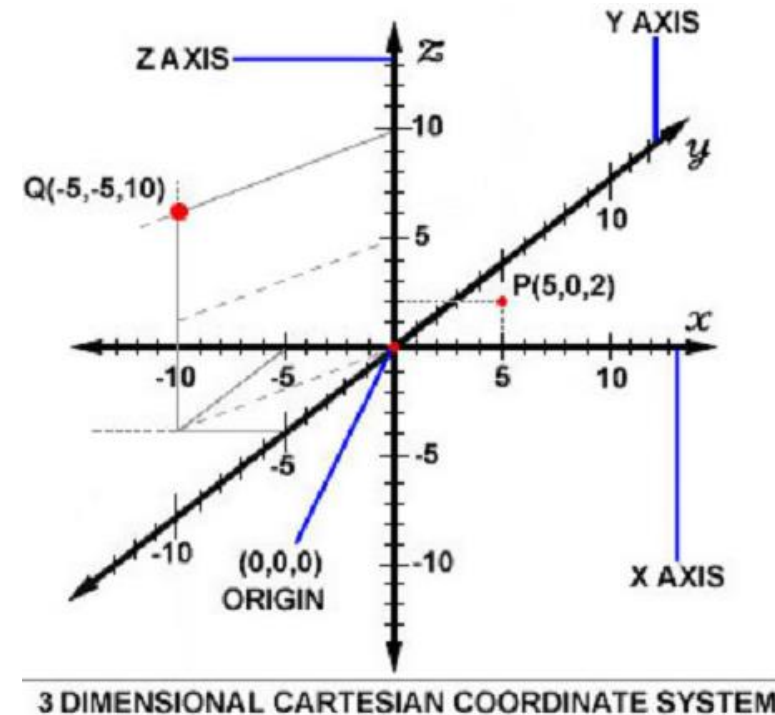
# Cartesian & Projected Systems



- A two or three dimensional coordinate system in which, in the top example, X measures East/West distance and Y measures North/South distance.

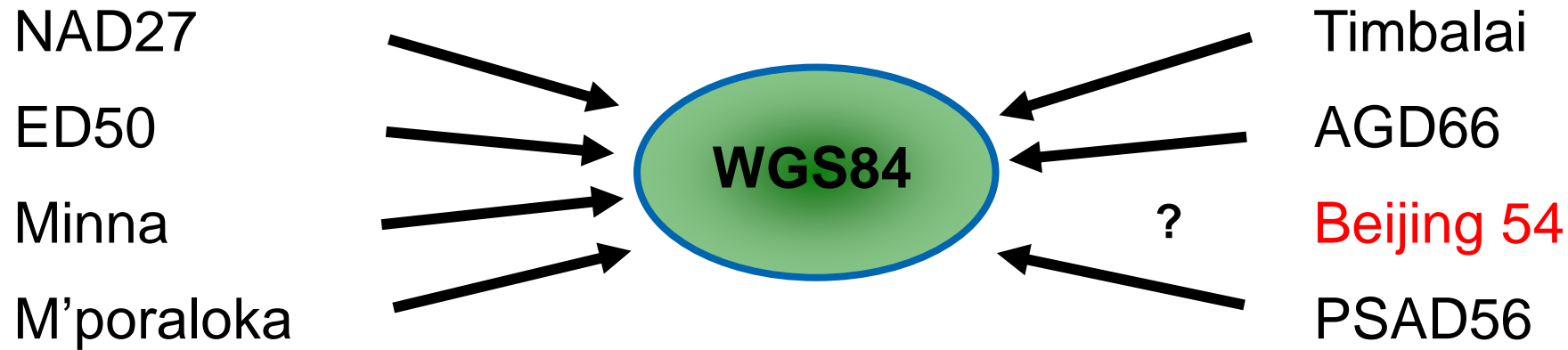
- Each point on the plane is defined by an X, Y, and sometimes Z coordinate pair. The point of intersection where the axes meet, is called the origin.

- Relative measures of distance, area, and direction are linear, and constant throughout the Cartesian system.



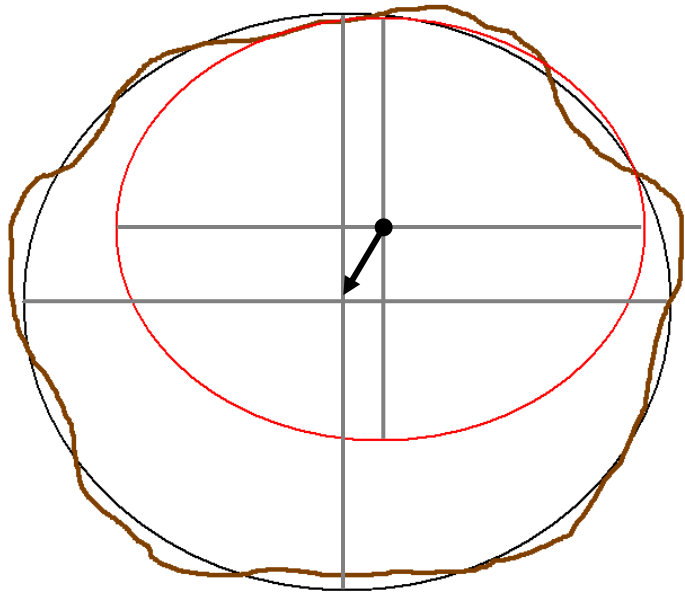
# WGS84 Ellipsoid/Datum

- World Geodetic System of 1984 is a standard ellipsoid definition worldwide
  - Earth-centered, a “best fit” for the whole earth
  - Originally created as Geodetic Reference System of 1980 by the US Defense Mapping Agency
  - Used as the basis worldwide for the GPS satellite network
  - It serves as a common ellipsoid/datum through which we convert most other datums



# Datum Transformations

- When coordinates exist on one datum, and the need exists to plot or display them based on another, a datum **transformation** is required.



## 3 Parameter shift (Molodensky, Geocentric):

- When performing a 3 parameter datum transformation, a linear shift is applied to the x, y, and z axes at the geocenter.
- Accuracy can be +/- 1 to 50 meters.
- Does not model network distortions well.
- But, they are easy to calculate!

## 7 Parameter Shift (Bursa-Wolfe, Helmert):

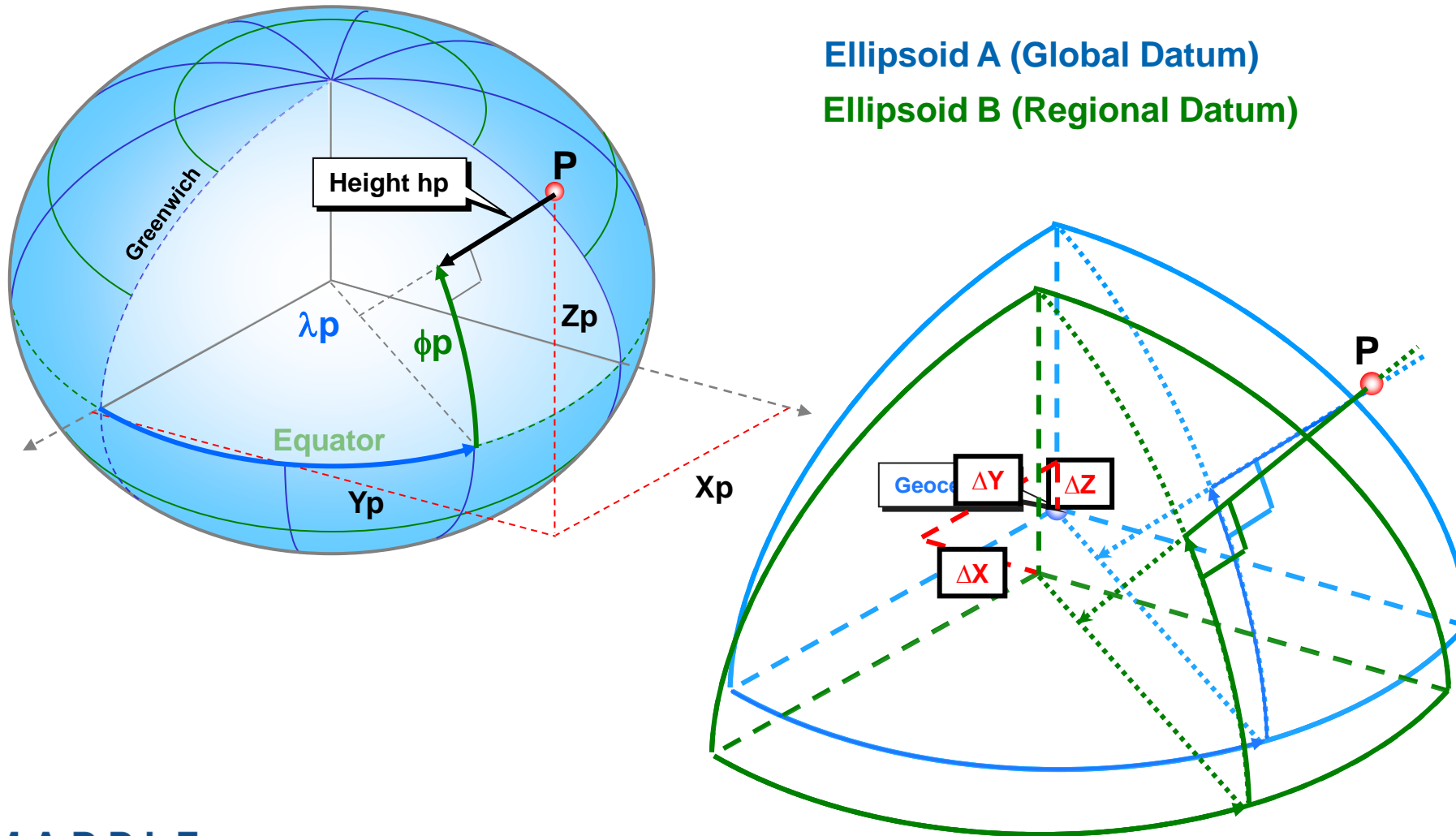
- The same x,y,z shift found in the Molodensky method, but with 3 additional parameters of rotations of the axes and a scale.
- If applied properly can allow for more accurate mapping of +/- 1m over large areas.
- Rotation sense is **critical**

## Other Transformation Methods (High Accuracy):

- Molodensky-Badekas 10 parameter (Rare)
- NADCON, HARN, NTv2, OSTN02, etc: (Gridded data tables)



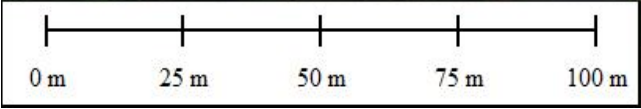
# What is a datum shift really?



# Datum Transformations – Example

## NAD 27 to WGS84

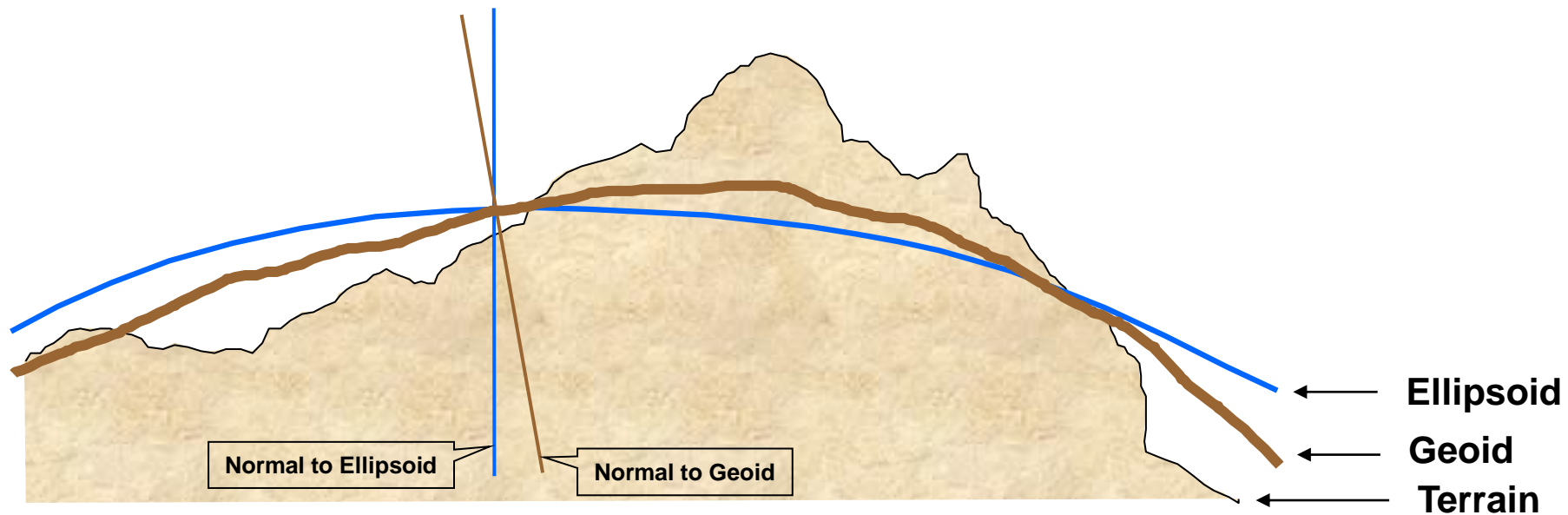
- NADCON (15cm)
- MRE (3m)
- Canadian NTV2 (3m)
- Molodensky
  - East US (13m)
  - Continental US (14.5m)



# Vertical Datums

## Geoid Model

- A **zero** surface to which elevations or heights are referred.
- Irregular surface model of the Earth that takes into account an average calculation of elevation factoring in ocean depth, gravimetric readings, and terrestrial height.



# Geoids and Mean Sea Level

## Geoid Model vs. MSL

- Not the same thing!
- Vertical models are *approximations* of MSL
  - Some are not sea level at all, but are actually tidal offsets, or some other local reference
- MSL is a “moving target”
  - For highest accuracy, local vertical deflections must be taken into account

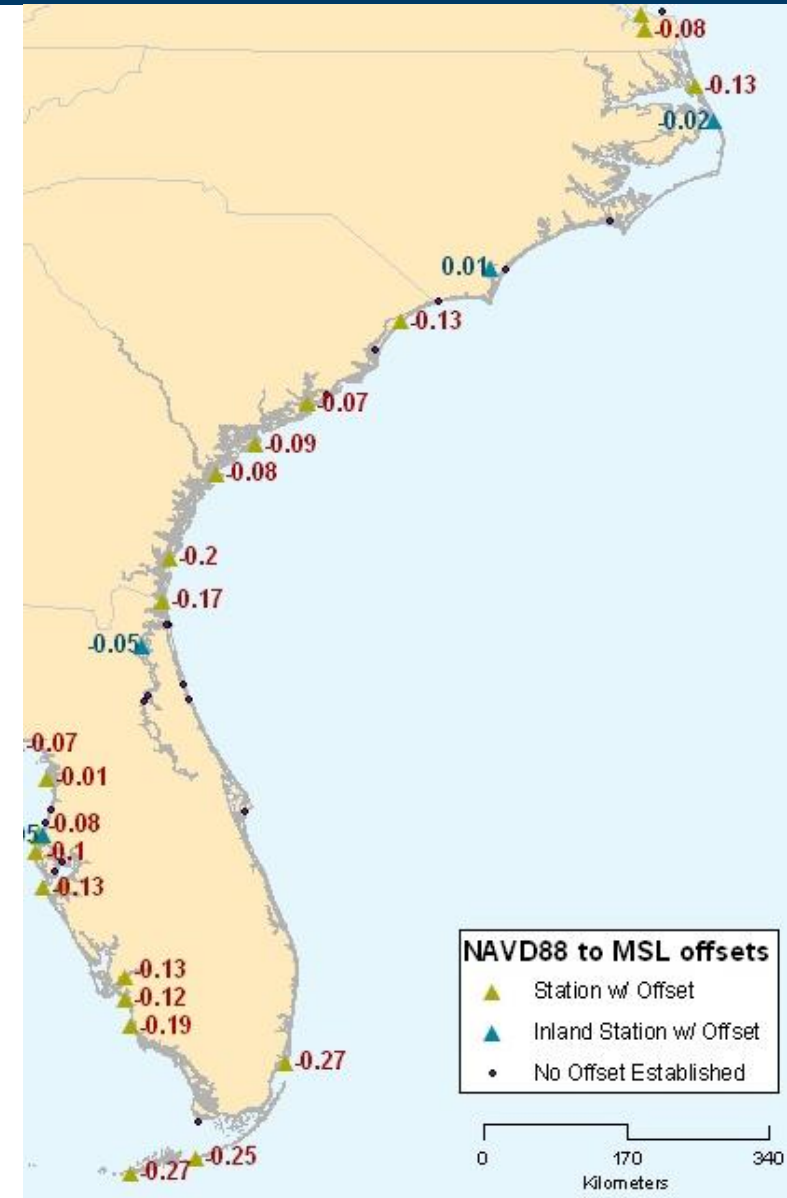


Image Courtesy of Seacoos.org

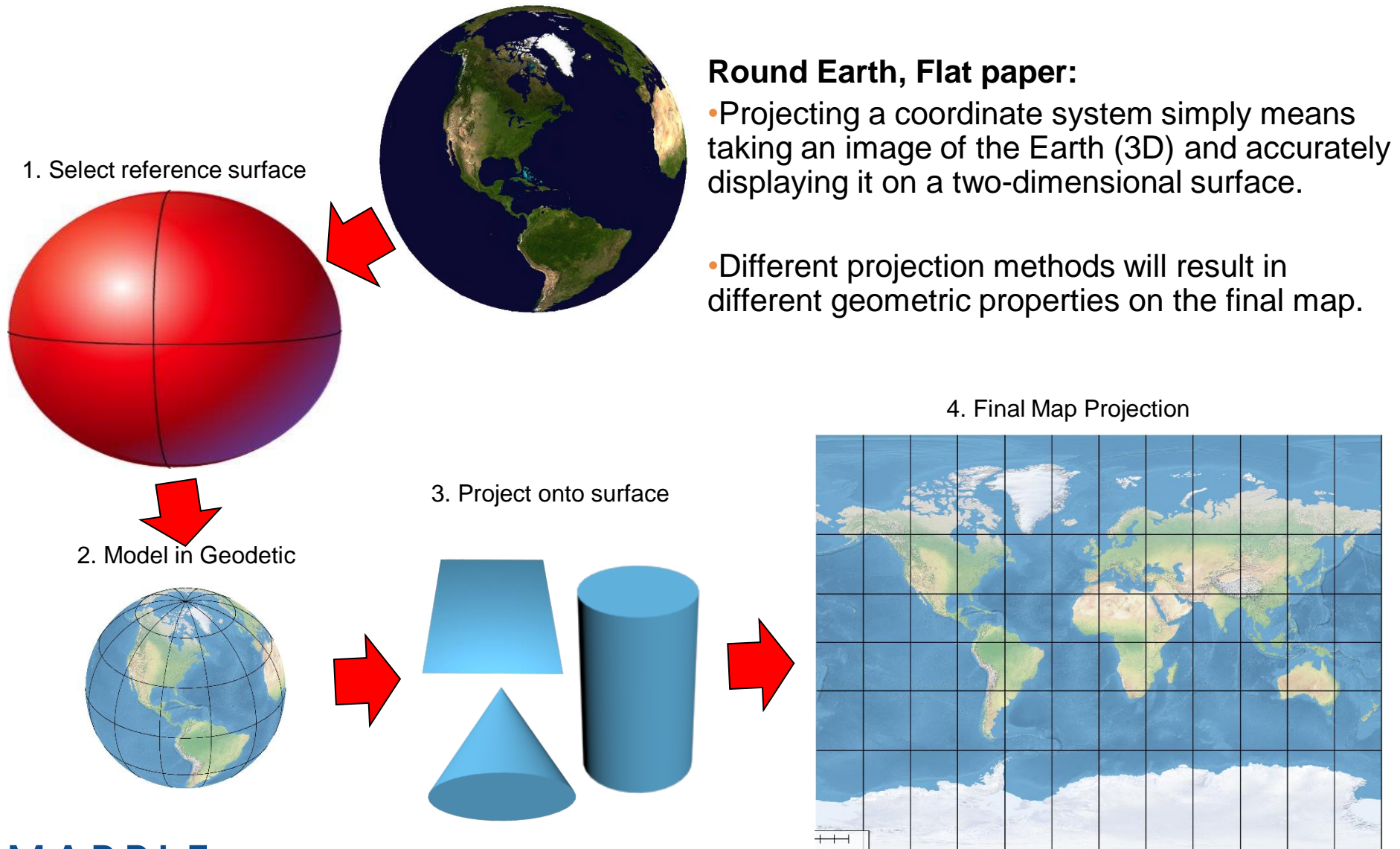


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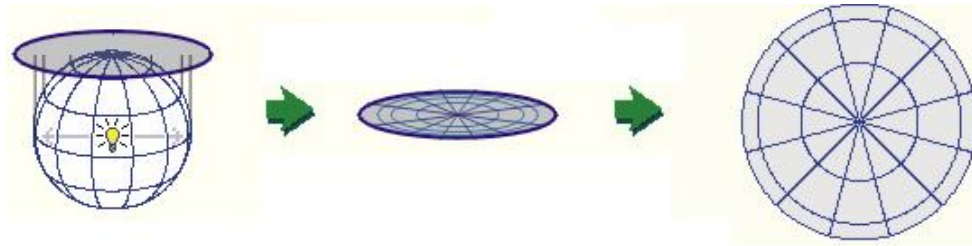
# Map Projections



# Projection Types

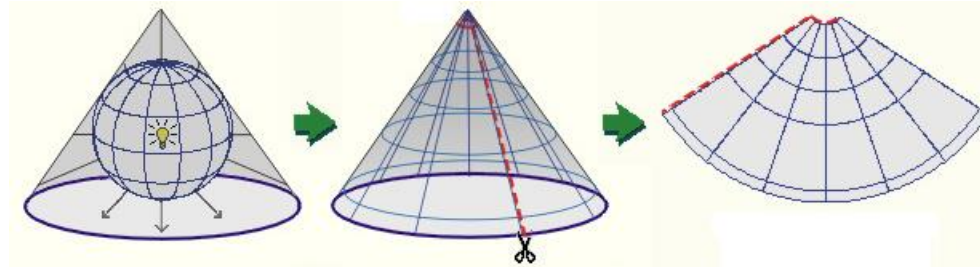
- **Azimuthal**

- The plane of projection touches the surface of the Earth at one point.



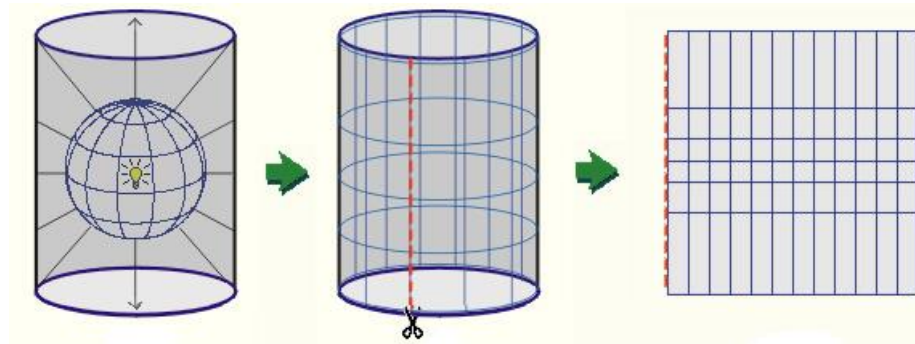
- **Conic**

- A cone shape is either tangent or secant to the globe, and the map is projected inside the cone.



- **Cylindrical**

- A cylinder is wrapped around the surface of the globe. The point of contact is a Great Circle.





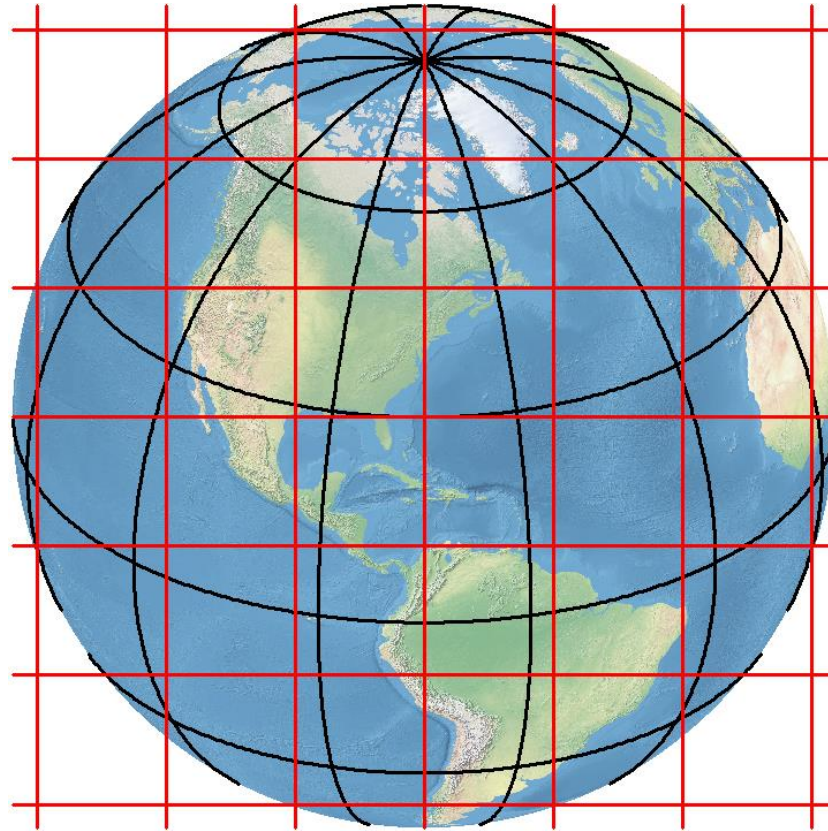
# Projection Properties

- **Equal Area**- Proportional preservation of surface areas. Linear and distance distortion occurs.
- **Equidistant**- Distances from the *center point* of the projection to any point (Great Circles) are preserved.
- **True Direction**- Rhumb lines represent true north azimuths. There is no convergence distortion.
- **Conformal**- Angles between points and shapes of small areas are preserved. The backbone of surveying coordinate systems.

# Projection Terms (cont'd)

- **Convergence**

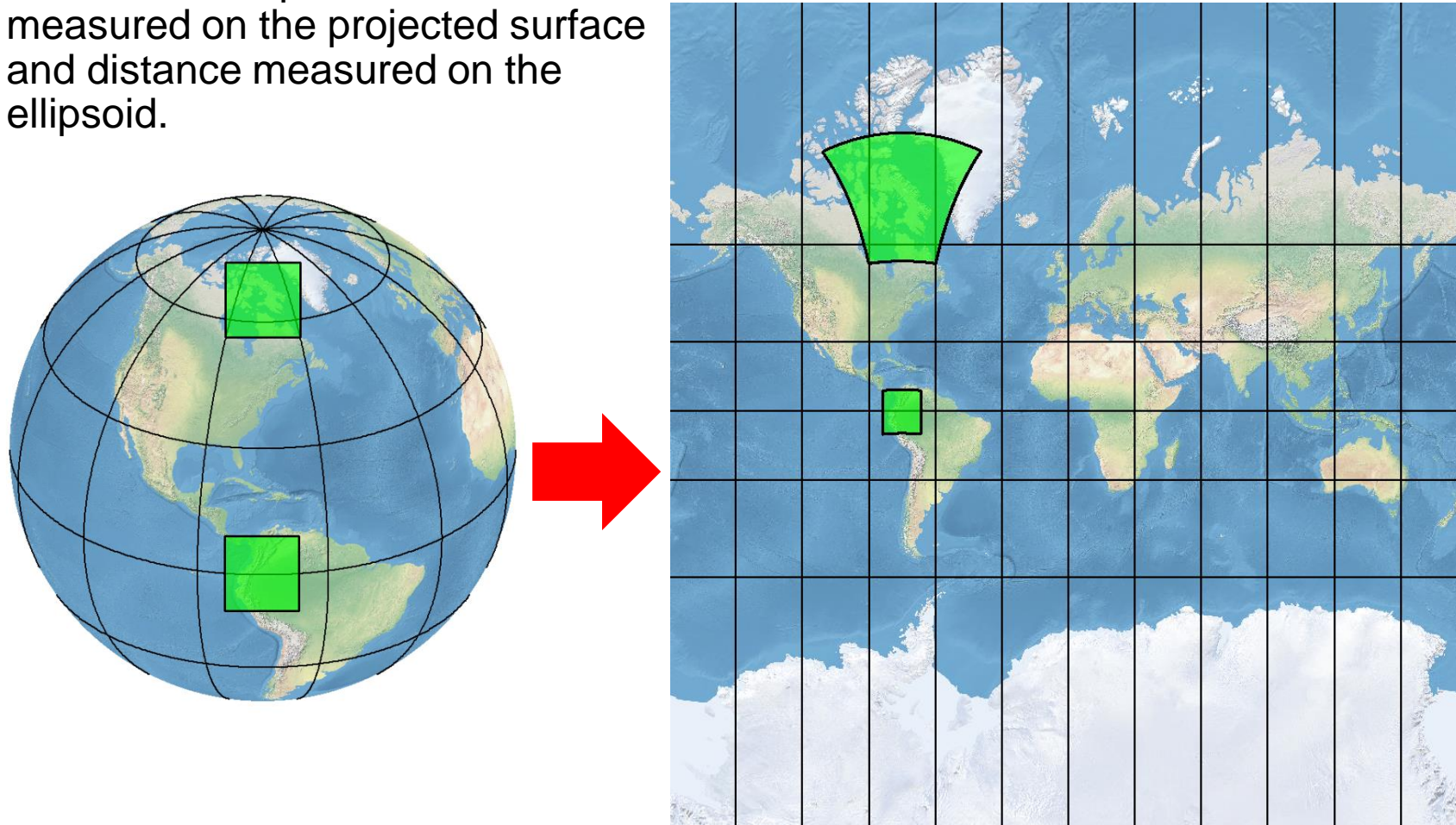
- The horizontal angle at a point between true North and Grid North.



# Projection Terms (cont'd)

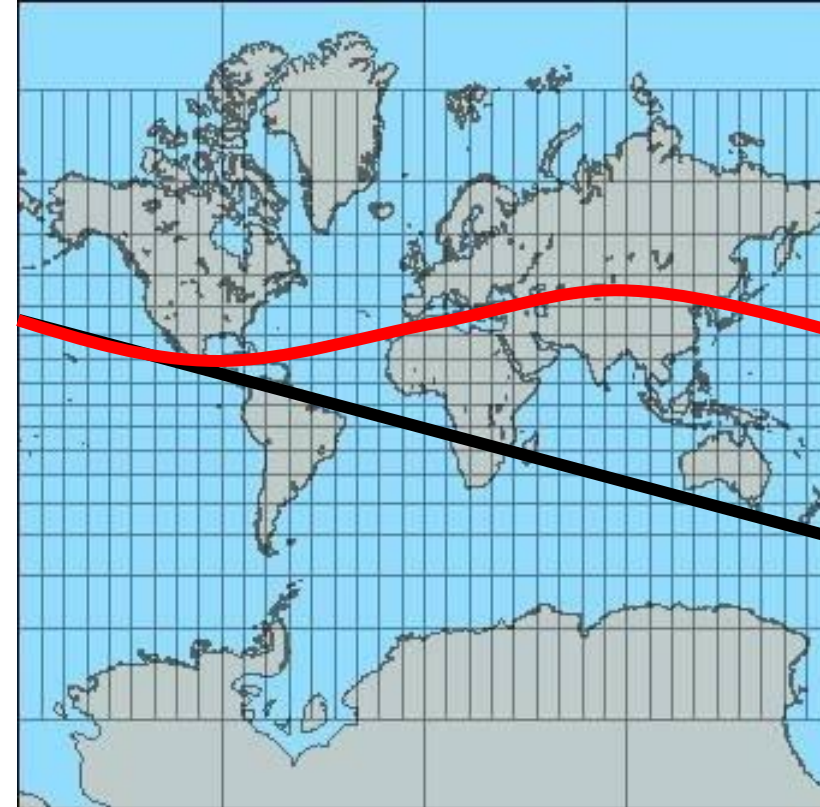
## Scale Factor

- The relationship between distance measured on the projected surface and distance measured on the ellipsoid.



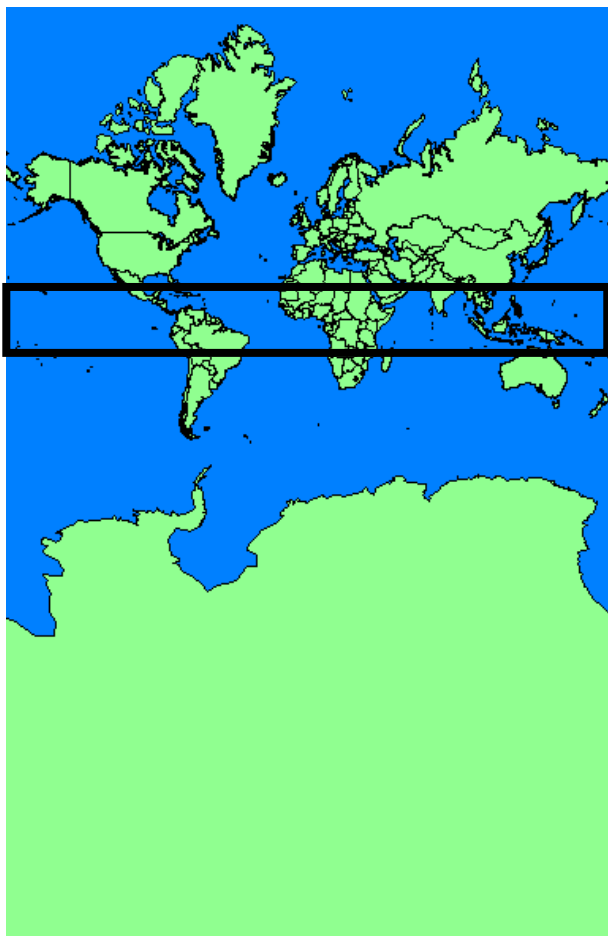
# Projection Terms

- **Azimuth**- Angle between North and direction of travel, measured clockwise from North.
  - Also called: Heading, Bearing, or Direction
- **Great Circle**- An arc that divides a sphere (in this case Earth) into two equal parts. Any line of Longitude (meridian) is a Great Circle.
- **Rhumb Line**- A line that intersects each meridian at the same angle.
  - Great for navigation





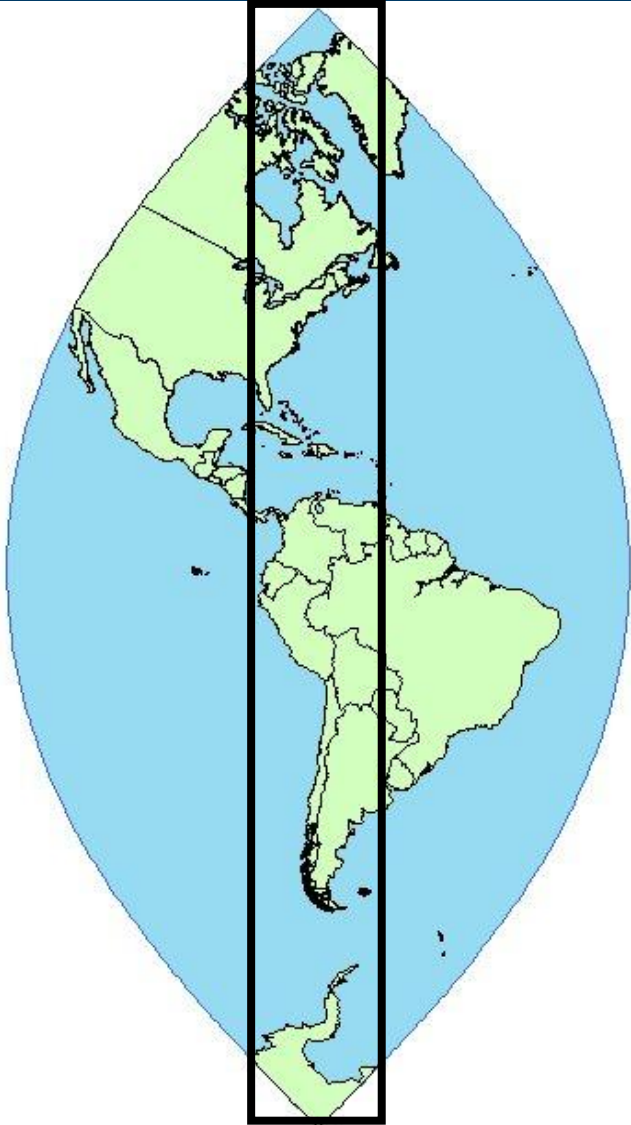
# Mercator Projection



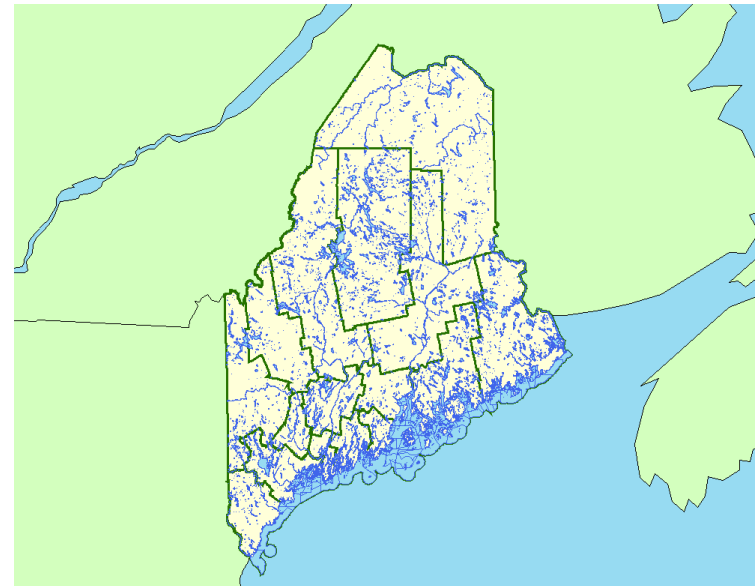
- Originally used for navigation.
- All meridians appear as parallel lines.
- Distances are true only along the Equator (or the parallel of origin), but are reasonably correct within  $15^\circ$  of the Equator
- Distortion increases further from the Equator and is extreme in polar regions.



# Transverse Mercator

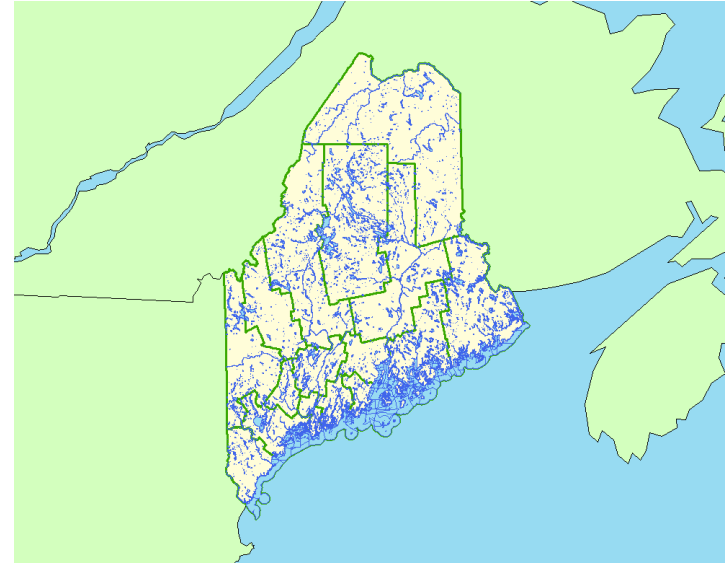
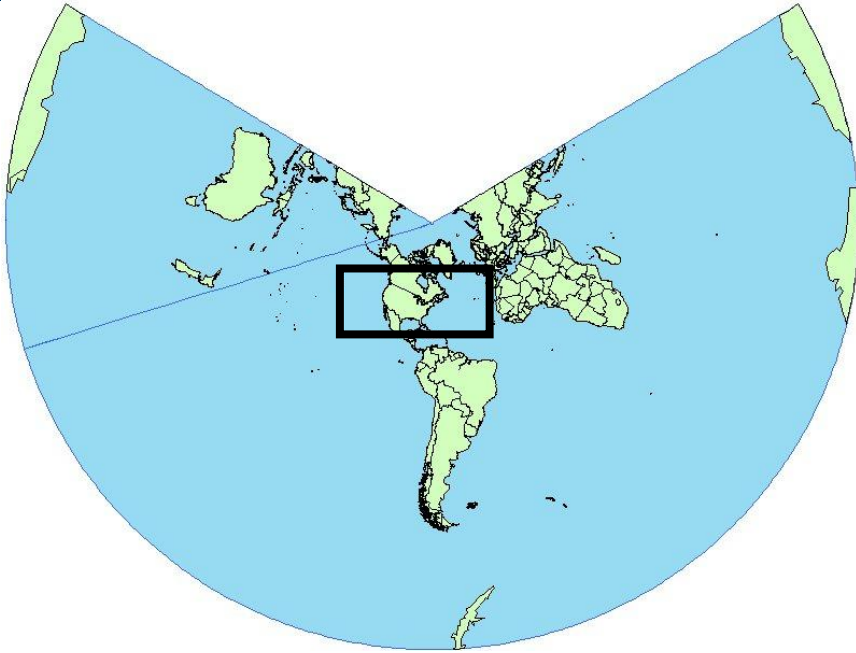


- Maps in this projection are used for mapping large areas that are mainly north-south in extent.
- Distances are true only along the central meridian, or two standard meridians.
- Used for most national grids, and of course Universal Transverse Mercator systems.





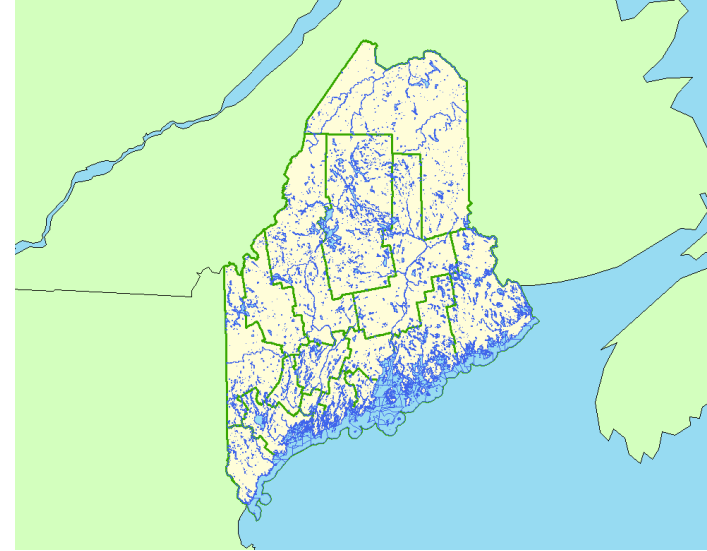
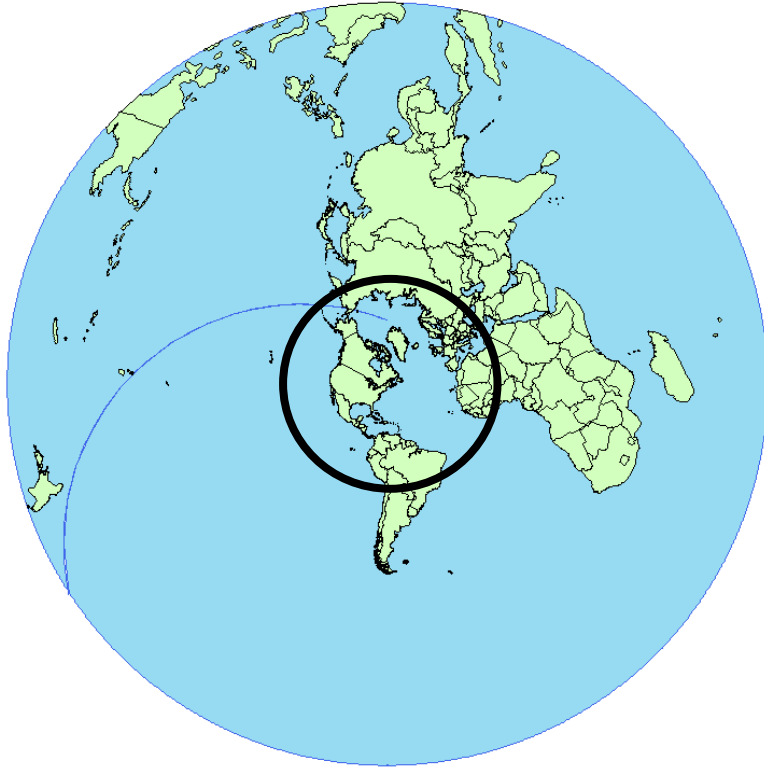
# Lambert Conformal Conic



- Used to show a region that has a greater East-West extent in middle latitudes
- Distances are true only along the two standard parallels (lines of contact) and are reasonably accurate elsewhere in limited regions.
- Distortion of shapes and areas is minimal at, but increases away from standard parallels.

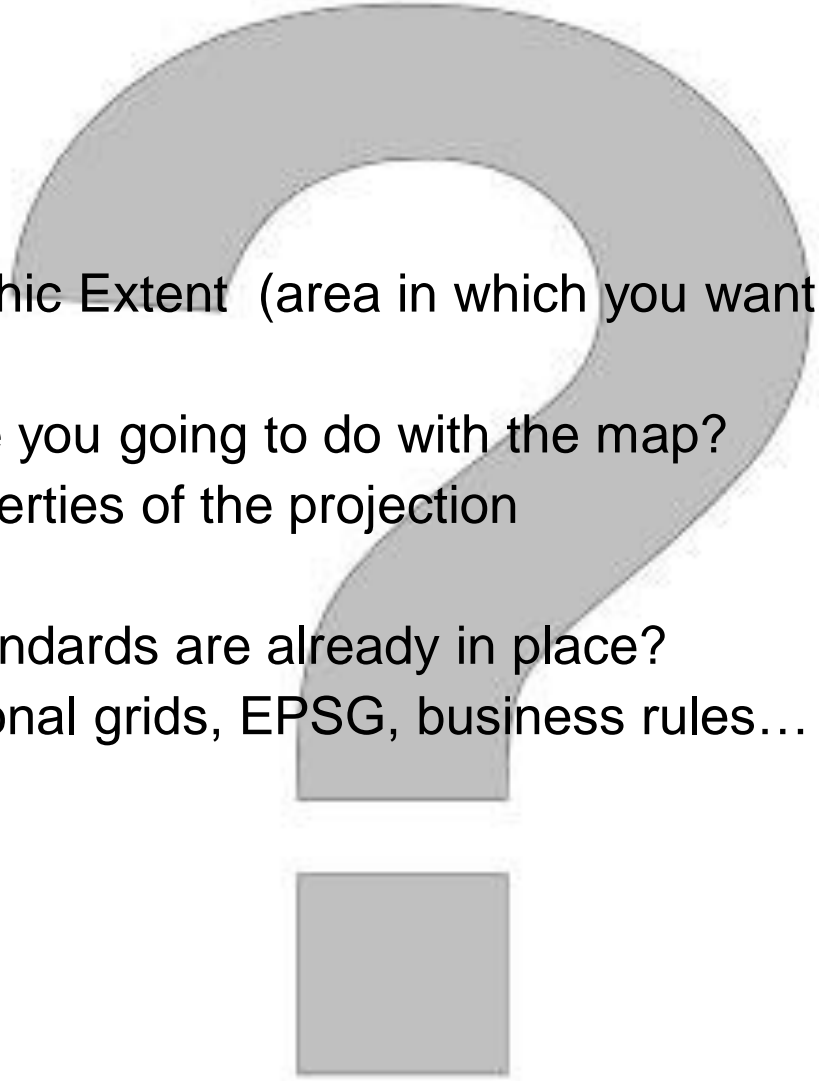


# Stereographic



- Used to map large continent-sized areas of similar extent in all directions.
- Polar aspects are used for topographic maps and charts for navigating in latitudes above  $80^\circ$ .
- Scale increases away from the center point.
- Any straight line through the center point is a great circle. Distortion of areas and large shapes increases away from center point.

# So Many Projections: How Do I Choose?

- 
- Geographic Extent (area in which you want to map)
  - What are you going to do with the map?
    - Properties of the projection
  - What standards are already in place?
    - National grids, EPSG, business rules...

# Further Reference

- NGS Video Library:  
[http://www.ngs.noaa.gov/corbin/class\\_description/NGS\\_Video\\_Library.shtml](http://www.ngs.noaa.gov/corbin/class_description/NGS_Video_Library.shtml)
- Book: Longitude: The True Story of a Lone Genius Who Solved the Greatest Scientific Problem of His Time by Dava Sobel
- Book: Datums and Map Projections: For Remote Sensing, GIS and Surveying, Second Edition *2nd Edition* by Jonathan Iliffe (Editor), Roger Lott (Editor)
- Book: Flattening the Earth: Two Thousand Years of Map Projections by John P Snyder



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**THANKS!**  
**QUESTIONS, DISCUSSION?**

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